

King Abdulaziz University  
Mechanical Engineering Department

MEP 460 Heat Exchanger Design

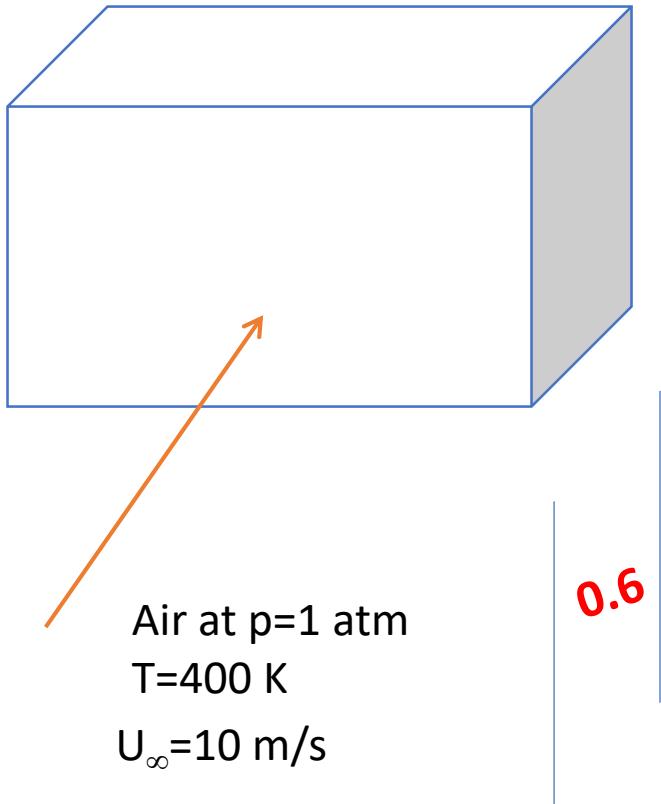
Compact Heat Exchangers  
Part 2

**Ch. 10 of Kakac textbook  
&  
Kays & London textbook  
Compact Heat Exchangers**

# **6-Examples (Kakac Textbook)**

## Example 10.1

Air at 1 atm and 400 K and with a velocity of  $U_{\infty} = 10 \text{ m/s}$  flows across a compact heat exchanger matrix having the configuration shown in Figure 10.4. Calculate the heat transfer coefficient,  $h$ , and frictional pressure drop for the air side. The length of the matrix is 0.6 m.



Find  $h$  and  $\Delta p$

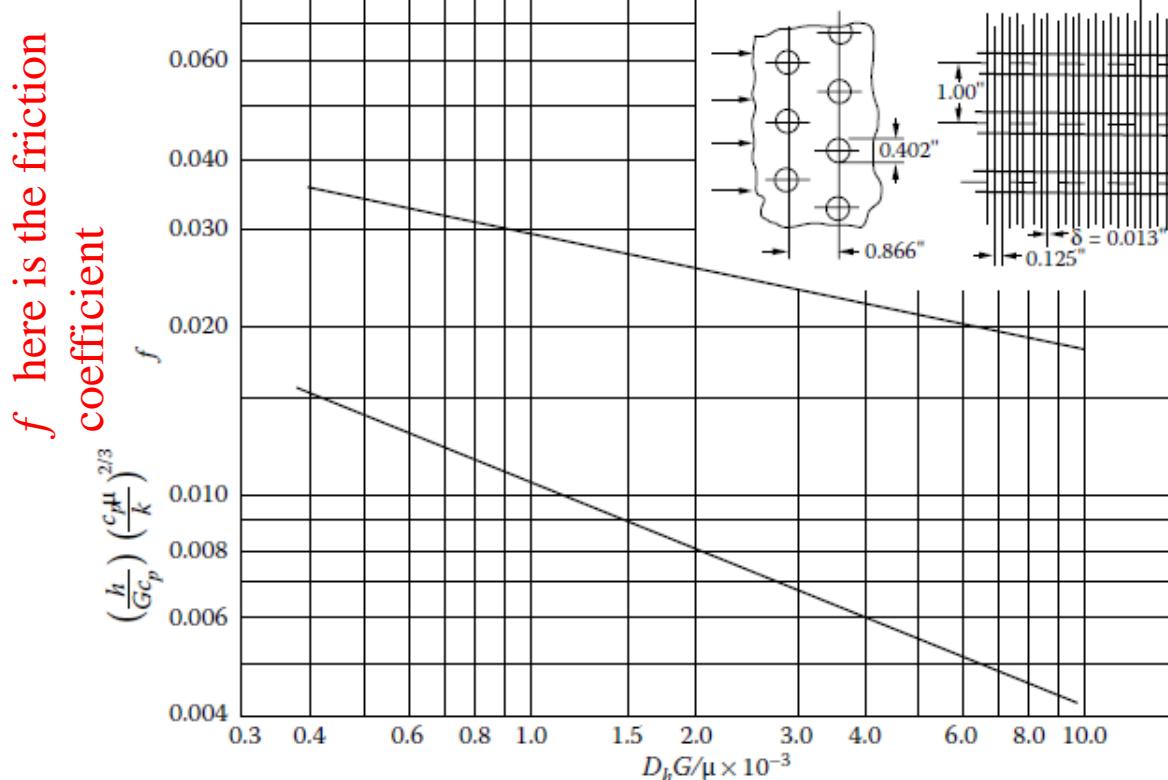


FIGURE 10.4

Heat transfer and friction factor for a circular tube continuous fin heat exchanger. Surface 8.0-3/8 T: tube OD = 1.02 cm; fin pitch = 3.15/cm; fin thickness = 0.033 cm; fin area/total area = 0.839; air-passage hydraulic diameter = 0.3633 cm; free-flow area/frontal area,  $\sigma = 0.534$ ; heat transfer area/total volume =  $587 \text{ m}^2/\text{m}^3$ . (From Kays, W. M. and London, A. L., *Compact Heat Exchangers*, 3rd ed., McGraw-Hill, New York, 1984. With permission.)

## Example 10.1

At 400 K and 1 atm, the properties of air from Appendix B are

$$\rho = 0.8825 \text{ kg/m}^3$$

$$\mu = 2.29 \times 10^{-5} \text{ kg/m}\cdot\text{s}$$

$$c_p = 1013 \text{ Jk/g}\cdot\text{K}$$

$$Pr = 0.719$$

$$G = \frac{\rho u_\infty A_{fr}}{A_{min}} = \frac{\rho u_\infty}{\sigma} = \frac{0.8825 \times 10}{0.534} = 16.53 \text{ kg/(m}^2\cdot\text{s})$$

$$Re = \frac{GD_h}{\mu} = \frac{16.53 \times 0.3633 \times 10^{-2}}{2.29 \times 10^{-5}} = 2622$$

**Example 10.1** From Figure 10.4, for  $Re = 2,622$ , we can obtain

$$\frac{h}{Gc_p} Pr^{2/3} = 0.0071$$

$$h = 0.0071 \times \frac{Gc_p}{Pr^{2/3}} = 0.0071 \times \frac{16.53 \times 10^3}{(0.719)^{2/3}}$$

$$h = 148.1 \text{ W/m}^2 \cdot \text{K}$$

For  $Re = 2,622$ , from Figure 10.4,  $f = 0.025$  and so

*f* here is the friction coefficient

$$\Delta p_f = f \frac{G^2}{2\rho_a} \frac{A_t}{A_{\min}}$$

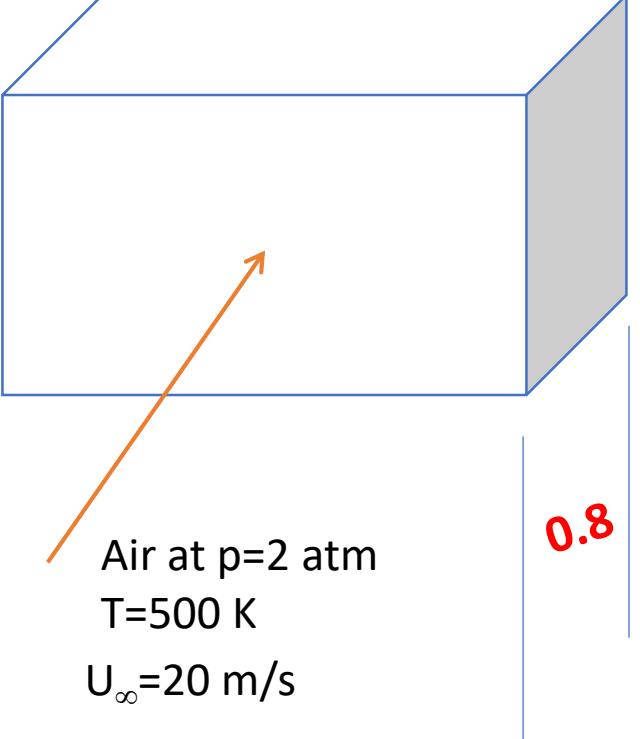
$$\frac{A_t}{A_{\min}} = \frac{4 \times L}{D_h} = \frac{4 \times 0.6}{0.3633 \times 10^{-2}} = 660.6$$

Then,

$$\Delta p_f = 0.025 \times \frac{16.53^2}{2 \times 0.8825} \times 660.6 = 2556 \text{ Pa}$$

## Example 10.2

Air at 2 atm and 500 K with a velocity of  $U_{\infty} = 20$  m/s flows across a compact heat exchanger matrix having the configuration shown in Figure 10.8 (surface [11.32-0737-S-R](#)). Calculate the heat transfer coefficient and the frictional pressure drop. The length of the matrix is 0.8 m.



Find  $h$  and  $\Delta p$

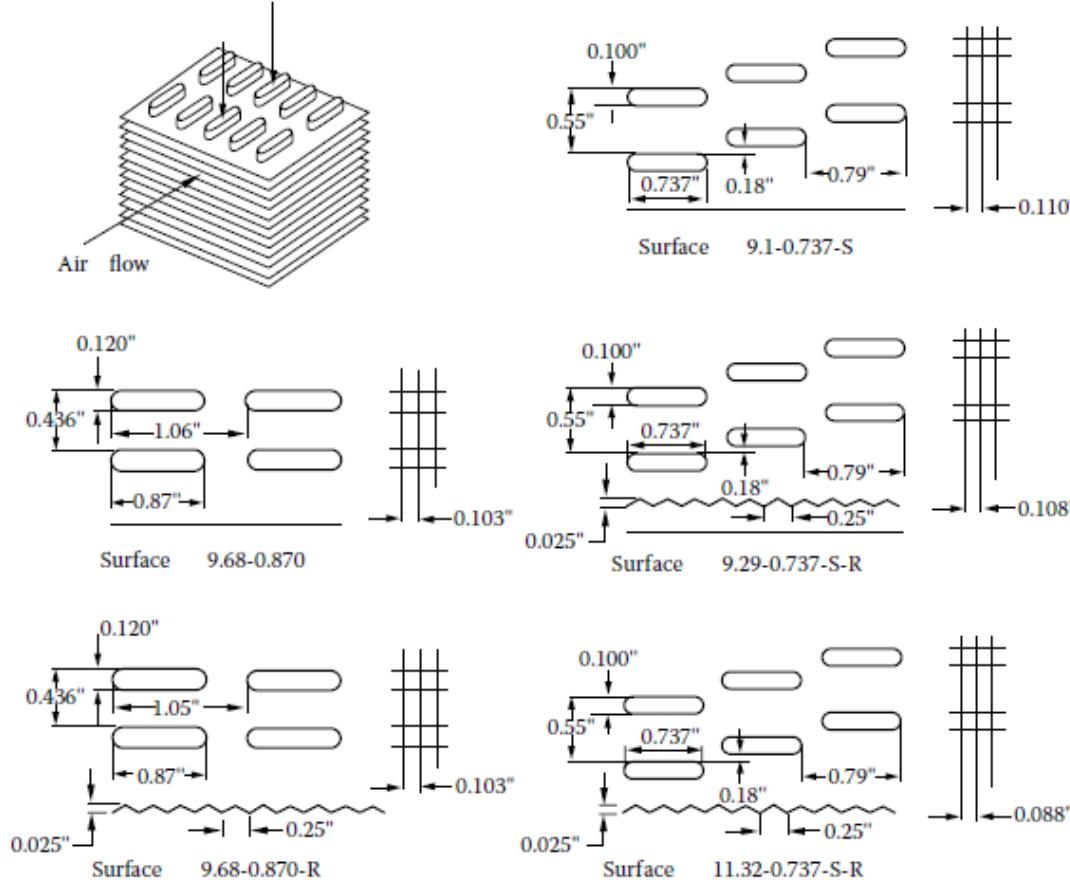


FIGURE 10.8

Various flattened tube-platefin compact surfaces for which test data are presented in Figure 10.7. (From Kays, W. M. and London, A. L., *Compact Heat Exchangers*, 3rd ed., McGraw-Hill, New York, 1984. With permission.)

## Example 10.2

TABLE 10.1

Heat Transfer Matrix Geometries for Plate Plain-Fin and Fin Flat-Tube Types for Which Test Data are Presented in Figures 10.7 and 10.9

Surface Designation	Fins (per cm)	Hydraulic Diameter ( $D_h$ , cm)	Plate Spacing ( $b$ , cm)	Tube or Fin Thickness (cm)	Extended Area		Area	Area	Free Flow Area
					Total Area	Volume Between Plates ( $\beta$ , m <sup>2</sup> /m <sup>3</sup> )			
<i>Plate plain-fin type</i>									
5.30	13.46	0.051	1.194	0.0152	0.719	511.8			
11.10	28.19	0.257	0.635	0.0152	0.730	1095.8			
14.77	37.52	0.215	0.838	0.0152	0.831	1210.6			
19.86	50.44	0.152	0.635	0.0152	0.833	1493.0			
<i>Fin flat-tube type</i>									
9.68-0.870	24.587	0.2997		0.0102	0.795		751.3	0.697	
9.68-0.870-R	24.587	0.2997		0.0102	0.795		751.3	0.697	
9.1-0.737-S	23.114	0.3565		0.0102	0.813		734.9	0.788	
9.29-0.737-S-R	28.753	0.3510		0.0102	0.845		885.8	0.788	
11.32-0.737-S-R	23.596	0.3434		0.0102	0.814		748.0	0.780	

Source: From Kays, W. M. and London, A. L., *Compact Heat Exchangers*, 3rd ed., McGraw-Hill, New York, 1984. With permission.

# Flat tube 11.32-0.737S-R

(c) Flat tubes, continuous fins

Surface designation	Tube arrangement	Fin type	Tube length (parallel to flow)		Tube width (normal to flow)		Fins/in	Hydraulic diameter $4r_h$		Fin thickness $\delta$		Free flow/ frontal area $\sigma$	Heat transfer area/ total volume $\alpha$		Fin area/ total area
			in	$10^{-3}\text{m}$	in	$10^{-3}\text{m}$		ft	$10^{-3}\text{m}$	in	$10^{-3}\text{m}$	$\text{ft}^2/\text{ft}^3$	$\text{m}^2/\text{m}^3$		
9.68-0.87	In-line	Plain	0.870	22.1	0.120	3.0	9.68	0.01180	3.60	0.004	0.102	0.697	229	751	0.795
9.1-0.737S	Staggered	Plain	0.737	18.7	0.100	2.5	9.1	0.01380	4.21	0.004	0.102	0.788	224	735	0.813
9.68-0.87R	In-line	Ruffled	0.870	22.1	0.120	3.0	9.68	0.01180	3.60	0.004	0.102	0.697	229	751	0.795
9.21-0.737SR	Staggered	Ruffled	0.737	18.7	0.100	2.5	9.29	0.01352	4.12	0.004	0.102	0.788	228	748	0.814
11.32-0.737SR	Staggered	Ruffled	0.737	18.7	0.100	2.5	11.32	0.01152	3.51	0.004	0.102	0.780	270	886	0.845

Kays and London  
Compact Heat Exchangers, 3ed edition

## Example 10.2

The mass flux  $G$  is

$$G = \frac{\dot{m}}{A_{\min}} = \frac{\rho u_{\infty} A_{fr}}{A_{\min}} = \frac{\rho u_{\infty}}{\sigma} = \frac{1.41 \times 20}{0.78} = 36.15 \text{ kg/m}^2 \cdot \text{s}$$

$$Re = \frac{GD_h}{\mu} = \frac{36.15 \times 0.3434 \times 10^{-2}}{2.69 \times 10^{-5}} = 4615$$

From Figure 10.7, for  $Re = 4,615$ , we get

$$\frac{h}{Gc_p} \cdot Pr^{2/3} = 0.0058$$

$$h = 0.0058 \frac{Gc_p}{Pr^{2/3}}$$

$$h = 0.0058 \times \frac{36.15 \times 1030}{(0.718)^{2/3}} = 278.7 \text{ W/m}^2 \cdot \text{K}$$

$$\Delta p_f = f \frac{A_t}{A_{\min}} \frac{\rho_i}{\rho} \frac{G^2}{2\rho_i}$$

$$\frac{A_t}{A_{\min}} = \frac{4 \times L}{D_h} = \frac{4 \times 0.8}{0.3434 \times 10^{-2}} = 932$$

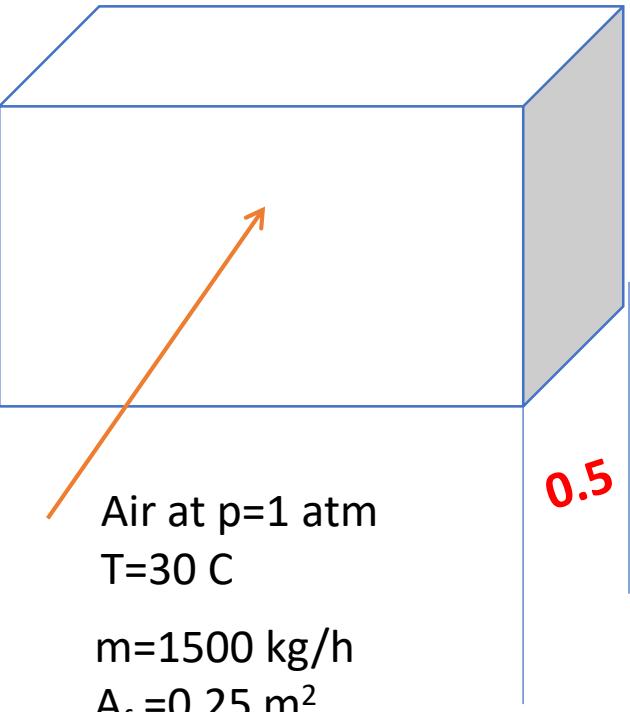
*f* here is the friction coefficient

For  $Re = 4,615$ , from Figure 10.7,  $f = 0.023$  and  $\rho_i/\rho_o \approx 1$ :

$$\Delta p_f = 0.023 \times 932 \times \frac{(36.15)^2}{2 \times 1.41} = 9934 \text{ N/m}^2$$

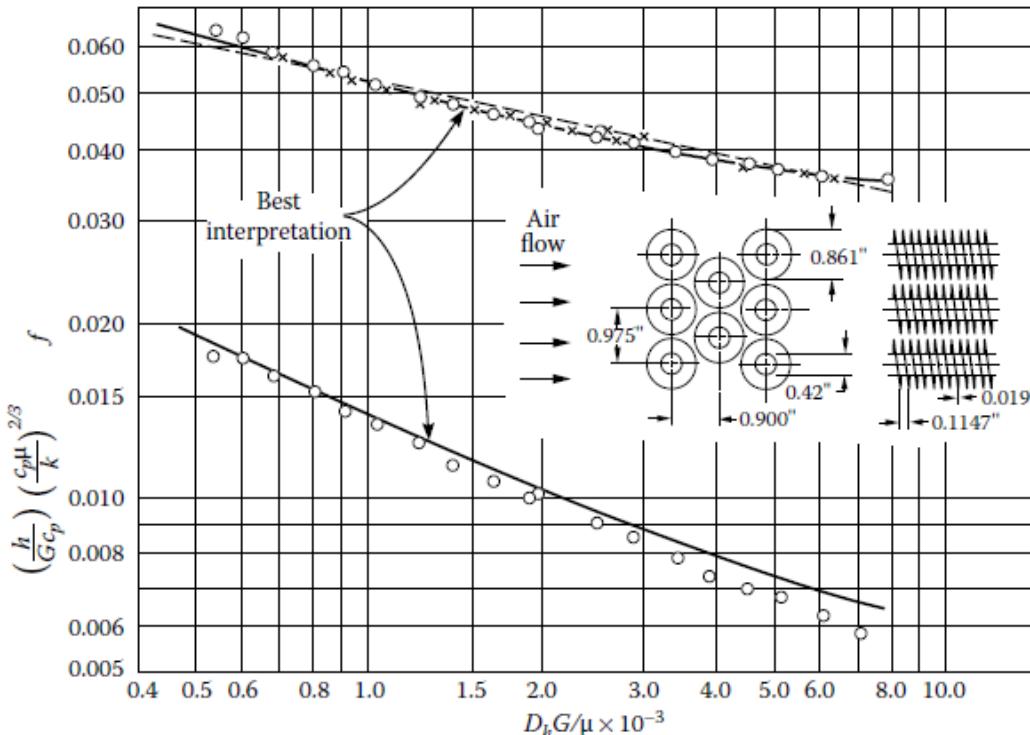
### Example 10.3

Air enters the core of a finned-tube heat exchanger of the type shown in Figure 10.5 at 1 atm and 30°C. The air flows at a rate of 1,500 kg/h perpendicular to the tubes and exits with a mean temperature of 100°C. The core is 0.5 m long with a 0.25 m<sup>2</sup> frontal area. Calculate the total pressure drop between the air inlet and outlet and the average heat transfer coefficient on the air side.  $T_o = 100^\circ\text{C}$



Find  $h$  and  $\Delta p$

$f$  here is the friction coefficient



Surface: CF-8.72C

FIGURE 10.5  
Heat transfer and friction factor for flow across circular finned-tube matrix. Surface CF-8.72(c): tube OD = 1.07 cm; fin pitch = 3.43/cm; fin thickness = 0.048 cm; fin area/total area = 0.876; air-passage hydraulic diameter,  $d_h = 0.443 \text{ cm}$ ; free-flow area/frontal area,  $\sigma = 0.494$ ; heat transfer area/total volume = 446 m<sup>2</sup>/m<sup>3</sup>. (From Kays, W. M. and London, A. L., *Compact Heat Exchangers*, 3rd ed., McGraw-Hill, New York, 1984. With permission.)

## Example 10.3

$$\rho_i = 1.177 \text{ kg/m}^3$$

$$\rho_o = 0.954 \text{ kg/m}^3$$

$$\frac{A_t}{A_{\min}} = \frac{4L}{D_h} = \frac{4 \times 0.5}{0.00443} = 451.5$$

$$A_{\min} = \sigma A_f = 0.494 \times 0.25 = 0.124 \text{ m}^2$$

$$G = \frac{\dot{m}}{A_{\min}} = \frac{1500}{3600} \times \frac{1}{0.124} = 3.36 \text{ kg/m}^2 \cdot \text{s}$$

$$Re = \frac{GD_h}{\mu} = \frac{3.36 \times 0.00443}{2.04 \times 10^{-5}} = 729$$

## Example 10.3

$$\begin{aligned}\Delta p &= (3.36)^2 \frac{1}{2 \times 1.177} \left[ 0.057 \times 451.5 \times \frac{1.177}{1.038} + (1 + 0.494^2) \left( \frac{1.177}{0.954} - 1 \right) \right] \\ &= 141.3 \text{ N/m}^2\end{aligned}$$

For the heat transfer coefficient, the Colburn modulus ( $h/Gc_p$ )  $Pr^{2/3}$  can be read from Figure 10.5 for  $Re = 729$  as 0.0165.

$$\frac{h}{Gc_p} Pr^{2/3} = 0.0165$$

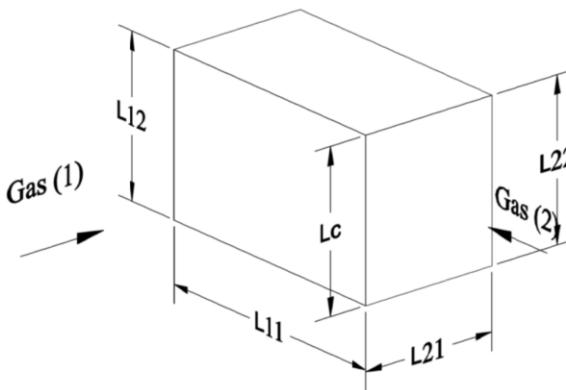
$$h = 0.0165 \times 3.36 \times 1.007 \times 10^3 \times (0.719)^{-2/3}$$

$$h \approx 70 \text{ W/m}^2 \cdot \text{K}$$

Input data sheet for rating Gas-to-Gas compact heat exchanger

Solved example. Reference: Kays & London 3ed edition

#	Symbol	Meaning	Value	Unit	Remarks
1	Fluid 1	Gas side (1) fluid	Air	-	
2	L11	Length 1 of HE $\perp$ to flow 1	0.91	m	
3	L12	Length 2 of HE $\perp$ to flow 1	2.29	m	
4	$\dot{m}_1$	mass flow rate of flow 1	24.3	kg/s	Either the mass flow rate
5	$\dot{V}_1$	volumetric flow rate in side (1)	--	$\text{m}^3/\text{s}$	or volume flow rate is given
6	$P_{i,1}$	inlet pressure of flow (1)	$9.1 \times 10^5$	Pa	
7	$T_{i,1}$	inlet temperature of flow (1)	175	$^\circ\text{C}$	
8	mat1\$	matrix designation for side (1)	3/8-6.06	-	Louvered fin
9	$k_{f1}$	fin side (1) thermal conductivity of	21.24	W/m.K	
10	a	plate thickness	$0.3 \times 10^{-3}$	m	
11	Fluid 2	Gas side (2) fluid	gas (Air)	-	
12	L21	Length 1 of HE $\perp$ to flow 2	1.83	m	
13	L22	Length 2 of HE $\perp$ to flow 2	2.29	m	
14	$\dot{m}_2$	mass flow rate of flow 2	24.7	kg/s	
15	$\dot{V}_2$	volumetric flow rate in side (2)	--	$\text{m}^3/\text{s}$	
16	$P_{i,2}$	inlet pressure of flow (2)	$103 \times 10^3$	Pa	
17	$T_{i,2}$	inlet temperature of flow (2)	430	$^\circ\text{C}$	
18	mat2\$	matrix designation for side (2)	11.1	-	
19	$k_{f2}$	fin side (2) thermal conductivity of	21.24	W/m.K	
20	$k_p$	thermal conductivity of the plate	190	W/m.K	



## Solved example. Reference: Kays &amp; London 3ed edition

#	Symbol	Description	Source	Value	Units
1	Fluid 1	Gas side (1) fluid	Input data	Air	-
2	L11	Length 1 of HE $\perp$ to flow 1	Input data	0.91	m
3	L12	Length 2 of HE $\perp$ to flow 1	Input data	2.29	m
4	$\dot{m}_1$	mass flow rate of flow 1	Input data	24.3	kg/s
5	$\dot{V}_1$	volumetric flow rate into side (1)	Input data	-	$m^3/s$
6	P <sub>i,1</sub>	inlet pressure of flow (1)	Input data	$9.1 \times 10^5$	Pa
7	T <sub>i,1</sub>	inlet temperature of flow (1)	Input data	175	°C
8	mat1\$	surface designation for side (1)	Input data	3/8-6.06	-
9	k <sub>f1</sub>	fin side (1) thermal conductivity of	Input data	21.24	W/m.K
10	a	plate thickness	Input data	$0.3 \times 10^{-3}$	m
					m
11	b <sub>1</sub>	Plate spacing (1)	surface data	$6.35 \times 10^{-3}$	m
12	D <sub>h1</sub>	Hydraulic diameter (1)	surface data	$4.453 \times 10^{-3}$	m
13	$\delta_{f1}$	fin (1) thickness	surface data	$0.15 \times 10^{-3}$	$m^2/m^3$
14	$\beta_1$	heat transfer area/volume between the plates= $A_1/\nabla_{p1}$	surface data	840	$m^2/m^2$
15	$\omega_1$	fin (1) area / heat transfer area= $A_{f1}/A_1$	surface data	0.640	m
16	$l_{f1}$	fin (1) length	surface data (b <sub>1</sub> /2)	$3.175 \times 10^{-3}$	m
17	Fluid 2	Gas side (2) fluid	Input data	Gas (Air)	
18	L21	Length 1 of HE $\perp$ to flow 2	Input data	1.83	m
19	L22	Length 2 of HE $\perp$ to flow 2	Input data	2.29	m
20	$\dot{m}_2$	mass flow rate of flow 2	Input data	24.7	kg/s
21	$\dot{V}_2$	volumetric flow rate in side (2)	Input data	--	$m^3/s$
22	P <sub>i,2</sub>	inlet pressure of flow (2)	Input data	$103 \times 10^3$	Pa
23	T <sub>i,2</sub>	Inlet temperature of gas into side (2)	Input data	430	C
24	mat2\$	Surface (2) designation	Input data	11.1	-
25	k <sub>f2</sub>	fin (2) thermal conductivity	Input data	21.24	W/m.K
26	k <sub>p</sub>	plate thermal conductivity	Input data	190	W/m.K
27	b <sub>2</sub>	Plate spacing (2)	surface data	$6.35 \times 10^{-3}$	m
28	D <sub>h2</sub>	Hydraulic diameter (2)	surface data	$3.085 \times 10^{-3}$	m
29	$\delta_{f2}$	fin (2) thickness	surface data	$0.15 \times 10^{-3}$	m
30	$\beta_2$	heat transfer area/volume between the plates= $A_2/\nabla_{p2}$	surface data	1204	$m^2/m^3$
31	$\omega_2$	fin (2) area / heat transfer area= $A_{f2}/A_2$	surface data	0.756	$m^2/m^2$
32	$l_{f2}$	fin (2) length	surface data	$3.175 \times 10^{-3}$	m

#	Symbol	Description	Source	Value	Units
33	$\Delta T_o$	Inlet temperature difference	$T_{hi} - T_{ci} = <7> - <23>$	255	°C
34	$L_{p1}$	HX length // to flow (1)	Input data	1.83	m
35	$L_{p2}$	HX length // to flow (2)	Input data	0.91	m
35a	$L_c$	Common edge length	Input data	2.29	m
36	$A_{fr1}$	frontal area of side (1)	$L11 * L12 = <2> * <3>$	2.0839	$m^2$
37	$A_{fr2}$	frontal area of side (2)	$L21 * L22 = <18> * <19>$	4.1807	$m^2$
38	$N_p$	Number of plates $(L_c - b_1 - 2a) / (b_1 + b_2 + 2a)$	$<35a> - <11> - 2 <10>$ $<11> + <27> + 2 <10>$	172	-
39	$V_{p1}$	volume between the plates (1)	$L11 * L21 * b_1 * N_p = <2> * <18> * <11> * <38>$	1.815	$m^3$
40	$V_{p2}$	volume between the plates (2)	$L11 * L21 * b_2 * (N_p + 1) = <3> * <18> * <27> * (<38> + 1)$	1.825	$m^3$
41	$A_1$	heat transfer area of side (1)	$\beta_1 * V_{p1} = <14> * <39>$	1536.7	$m^2$
42	$A_2$	heat transfer area of side 2)	$\beta_2 * V_{p2} = <30> * <40>$	2198.3	$m^2$
43	$S_1 = A_{min,1}$	min. flow area of side (1) $Dh_1 * A_1 / 4L_{p1}$	$(<12> * <41>) / (4 <34>)$	0.9276	$m^2$
44	$S_2 = A_{min,2}$	min. flow area of side (2) $Dh_2 * A_2 / 4L_{p2}$	$(<28> * <42>) / (4 <35>)$	1.8675	$m^2$
45	$V$	Heat exchanger volume= $L11 * L12 * L_{p1}$	$<2> * <3> * <34>$	3.8135	$m^3$
45a	$A_1/A_2$	heat transfer area ratio	$(<41> / <42>)$	0.699	-
46	$\alpha_1$	heat transfer area (1)/HX volume	$<41> / <45>$	399.8	$m^2/m^3$
47	$\alpha_2$	heat transfer area (2)/HX volume	$<42> / <45>$	577.76	$m^2/m^3$
48	$\sigma_1$	side (1) min. flow area/frontal area (1)	$<43> / <36>$	0.4451	$m^2/m^2$
49	$\sigma_2$	side (2) min. flow area/frontal area (2)	$<44> / <37>$	0.444	$m^2/m^2$
50	$\rho_1$	density of gas (1) based on $P_{i,1}$ and $T_{i,1}$	Use $\rho = P_{i,1} / RT_{i,1}$	7.0775	$kg/m^3$
51	$\rho_2$	density of gas (2) based on $P_{i,2}$ and $T_{i,2}$	Use $\rho = P_{i,2} / RT_{i,2}$	0.5105	$kg/m^3$
52	$\dot{m}_1$	side (1) gas flow rate	Given or $\dot{V}_1 \rho_1 = <5> * <50>$	24.3	kg/s
53	$\dot{m}_2$	side (2) gas flow rate	Given or $\dot{V}_2 \rho_2 = <21> * <51>$	24.7	kg/s
54	$C_{p1}$	assumed specific heat side (1)	Interpolation for assumed average $T_1$	1020.7	J/kg.K
55	$C_{p2}$	assumed specific heat side (2)	Interpolation for assumed average $T_2$	1075.7	J/kg.K
56	$C_1$	mass capacity rate (1)	$\dot{m}_1 C_{p1} = <52> * <54>$	24803	W/K
57	$C_2$	mass capacity rate (2)	$\dot{m}_2 C_{p2} = <53> * <55>$	26569.8	W/K
58	$C_{min}$	min. mass capacity rate	Smallest of $C_1$ and $C_2$	24803	W/K
59	$C_r$	ratio of $C_{min}/C_{max}$	$C_{min}/C_{max}$	0.9335	-
60	$U_1$	Overall heat transfer coeff. base on side (1)	Estimated.	--	$W/m^2K$
			You can either assume $U_1$ or $\varepsilon$	--	
61	$NTU_1$	Number of transfer unit based on side (1)	$U_1 A_1 / C_{min} = <60> * <41> / <58>$	--	-
62	$\varepsilon$	initial guess for the HX effectiveness	Assumed or calculated	0.75	-
63	$Q_{max}$	Max. heat rate for the HX	$C_{min} * \Delta T_o = <58> * <33>$	6324765	W
63a	$Q$	Heat rate	$\epsilon Q_{max} = <62> * <63>$	4743573	
64	$T_{o1}$	outlet temperature for flow in side (1)	$T_{o1} = T_{i1} + Q / C_1 = <7> + <63a> / <56>$	366.25	°C
65	$T_{o2}$	outlet temperature for flow in side (2)	$T_{o2} = T_{i2} - Q / C_2 = <23> - <63a> / <57>$	251.5	°C

#	Symbol	Description	Source	Value	Units
66	$T_{av,1}$	Average temp. side (1) $(T_{i,1} + T_{o,1})/2$	$\langle 7 \rangle + \langle 64 \rangle / 2$	270.5	°C
67	$T_{av,2}$	Average temp. side (2) $(T_{i,2} + T_{o,2})/2$	$\langle 23 \rangle + \langle 65 \rangle / 2$	340.75	°C
68	$\rho_1$	Density side (1)	$\rho_1 = P_{i,1}/RT_{av,1}$	5.834	kg/m³
69	$C_{p1}$	Specific heat side (1)	Interpolation	1038.7	J/kg.K
70	$k_1$	Thermal conductivity side (1)	Interpolation	$43.5 \times 10^{-3}$	W/m.K
71	$\mu_1$	Viscosity side (1)	Interpolation	$286 \times 10^{-7}$	Pa.s
72	$Pr_1$	Prandtl number side (1)	Interpolation	0.6831	-
73	$\rho_2$	Density side (2)	$\rho_2 = P_{i,2}/RT_{av,2}$	0.5847	kg/m³
74	$C_{p2}$	Specific heat side (2)	Interpolation	1053.82	J/kg.K
75	$k_2$	Thermal conductivity side (2)	Interpolation	$47.6 \times 10^{-3}$	W/m.K
76	$\mu_2$	Viscosity side (2)	Interpolation	$309.7 \times 10^{-7}$	Pa.s
77	$Pr_2$	Prandtl number side (2)	Interpolation	0.6862	-
78	$G_1$	Mass velocity of side (1) $G_1 = \dot{m}_1/S_1$	$\langle 52 \rangle / \langle 43 \rangle$	26.19	kg/s.m²
79	$Re_1$	Reynold's number side (1) $Re_1 = D_{h1}G_1/\mu_1$	$\langle 78 \rangle \times \langle 12 \rangle / \langle 71 \rangle$	4128.7	-
80	$J_1$	Heat transfer factor side (1)	Surface data	0.007317	-
81	$fc_1$	friction coefficient side (1)	Surface data	0.0372	-
82	$G_2$	Mass velocity of side (2) $G_2 = \dot{m}_2/S_2$	$\langle 53 \rangle / \langle 44 \rangle$	13.257	kg/s.m²
83	$Re_2$	Reynold's number side (2) $Re_2 = D_{h2}G_2/\mu_2$	$\langle 82 \rangle \times \langle 28 \rangle / \langle 76 \rangle$	1335.7	-
84	$J_2$	Heat transfer factor side (2)	Surface data	0.00457	-
85	$fc_2$	friction coefficient side (2)	Surface data	0.01591	-
86	$h_1$	Heat transfer coeff. side (1) $h_1 = J_1 G_1 C_{p1} Pr_1^{-2/3}$	$\langle 80 \rangle \times \langle 78 \rangle \times \langle 69 \rangle \times \langle 72^{-2/3} \rangle$	257.3	W/m²K
87	$h_2$	Heat transfer coeff. side (2) $h_2 = J_2 G_2 C_{p2} Pr_2^{-2/3}$	$\langle 84 \rangle \times \langle 82 \rangle \times \langle 74 \rangle \times \langle 77^{-2/3} \rangle$	82.95	W/m²K
88	$M_1$	Fin factor (1) $\sqrt{2h_1/k_{f1}\delta_{f1}}$	$\sqrt{2 \times 86} / (\langle 9 \rangle \times \langle 13 \rangle)$	401.54	1/m
89	$M_1 l_f$	Fin factor (1) * fin (1) length	$\langle 88 \rangle \times \langle 16 \rangle$	1.275	-
90	$\eta_{f1}$	Fin efficiency (1) $\eta_{f1} = \tanh(M_1 l_f) / M_1 l_f$	$\tanh(\langle 89 \rangle) / \langle 89 \rangle$	0.6707	-
91	$\eta_{01}$	Overall surface efficiency side (1)	$1 - \omega_1(1 - \eta_{f1})$ $1 - \langle 15 \rangle(1 - \langle 90 \rangle)$	0.790	-
92	$M_2$	Fin factor (2) $\sqrt{2h_2/k_{f2}\delta_{f2}}$	$\sqrt{2 \times 87} / (\langle 25 \rangle \times \langle 29 \rangle)$	227.45	1/m
93	$M_2 l_f$	Fin factor (2) * fin (2) length	$\langle 92 \rangle \times \langle 32 \rangle$	0.7221	-
94	$\eta_{f2}$	Fin efficiency (2) $\eta_{f2} = \tanh(M_2 l_f) / M_2 l_f$	$\tanh(\langle 93 \rangle) / \langle 93 \rangle$	0.856	-
95	$\eta_{02}$	Overall surface efficiency side (2)	$1 - \omega_2(1 - \eta_{f2})$ $1 - \langle 31 \rangle(1 - \langle 94 \rangle)$	0.89	-

#	Symbol	Description	Source	Value	Units
95a	A <sub>w</sub>	Wall area of all plates	$L11*L21*2(N_p+1)$ $\text{=<2><18>*2(<38>+1)}$	576.2	m <sup>2</sup>
96	R <sub>w</sub>	Wall thermal resistance	$a/k_p A_w$ $\text{=<10>/(<26><95a>)}$	$2.74*10^{-8}$	
97	U <sub>1</sub>	Overall heat transfer Coeff. based on side (1)	$1/U_1 = 1/h_1 \eta_{01} + R_w A_1 + (A_1/A_2)/h_2 \eta_{02}$ $1/U_1 = 1/(<86><91>) + <96><41> + <45a>/(<87><95>)$	69.1	W/m <sup>2</sup> K
98	C <sub>1</sub>	Heat capacity rate for side (1)	$\text{=<52><69>}$	25240	W/K
99	C <sub>2</sub>	Heat capacity rate for side (2)	$\text{=<53><74>}$	26029	W/K
100	C <sub>min</sub>	Min. heat capacity rate	Smallest of C <sub>1</sub> & C <sub>2</sub>	25240	W/K
101	C <sub>r</sub>	Ratio C <sub>min</sub> /C <sub>max</sub>	C <sub>min</sub> /C <sub>max</sub>	0.9696	-
102	NTU <sub>1</sub>	Number of transfer units based on side (1)	$NTU_1 = U_1 A_1 / C_1$ $NTU_1 = <97> * <41> / <98>$	4.207	-
103	$\epsilon$	HX effectiveness calculated or found from graph	Appropriate figure or expression	0.7388	-
104	Q <sub>max</sub>	Max. heat rate	$C_{min} \Delta T_o = <100><33>$	6436200	W
105	Q	Heat rate	$Q = \epsilon Q_{max} = <103><104>$	4755064	W
106	T <sub>o1</sub>	Outlet temperature for side (1)	$T_{o1} = T_{i1} + Q/C_1 = <7> + <105>/<98>$	363.4	°C
107	T <sub>o2</sub>	Outlet temperature for side (2)	$T_{o2} = T_{i2} - Q/C_2 = <23> - <105>/<99>$	247.3	°C
108	$\Delta P_1$	Pressure drop for flow in side (1)	$\Delta P_1 = 4f c_1 (L_{p1}/D_{h1}) G_1^2/(2\rho_1)$ $4 < 81 > (<34>/<12>)$ $<78>^2/(2 <68>)$	3591.6	Pa
109	$\Delta P_2$	Pressure drop for flow in side (2)	$\Delta P_2 = 4f c_2 (L_{p2}/D_{h2}) G_2^2/(2\rho_2)$ $4 < 85 > (<35>/<28>)$ $<82>^2/(2 <73>)$	2844.2	Pa

